Real photon structure at an $e^+e^-$ linear collider

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Abstract

Previous studies of the kinematic coverage for measuring the photon structure function $F_{2\gamma}$ at a future 500 GeV $e^+e^-$ linear collider [1, 2] are updated using current estimates of luminosities and important detector parameters. A simple illustration is given of the sensitivity of the photonic structure functions on the strong coupling constant $\alpha_s$. 
1 Kinematics

The basic kinematics of electron-photon \((e\gamma)\) deep-inelastic scattering (DIS) at an \(e^+e^-\) or \(e^-e^-\) collider is recalled in Fig. 1. Here and in what follows we consider only the electromagnetic one-photon-exchange process, i.e., it is assumed that QED radiative corrections and contributions due to the exchange of weak gauge bosons have been subtracted. For a recent study of neutral- and charged-current processes see ref. [4].

Figure 1: The kinematics of inclusive electromagnetic electron scattering off (quasi-)real photons in \(e^+e^-\) or \(e^-e^-\) collisions.

The unpolarised \(e\gamma\) DIS cross section is, at lowest order in the electromagnetic coupling \(\alpha\),

\[
\frac{d\sigma(e\gamma \rightarrow eX)}{dE_{\text{tag}} \, d\cos\theta_{\text{tag}}} = \frac{4\pi\alpha^2 E_{\text{tag}}}{Q^4 y} \cdot \left[ \{1 + (1 - y)^2\} F_2^\gamma(x, Q^2) - y^2 F_L^\gamma(x, Q^2) \right].
\]

(1)

Here \(F_{2,L}^\gamma(x, Q^2)\) denote the structure functions of the real photon. The virtuality of the probing photon and the invariant mass of the hadronic final state are given by

\[
Q^2 \equiv -q^2 = 2E_b E_{\text{tag}}(1 - \cos \theta_{\text{tag}}),
\]

\[
W_{\text{had}}^2 = (q + p)^2.
\]

(2)
The scaling variables $x$ and $y$ read

$$x = \frac{Q^2}{Q^2 + W_{\text{had}}^2},$$

$$y = 1 - \frac{E_{\text{tag}}}{E_b} \cos^2 \left( \frac{\theta_{\text{tag}}}{2} \right).$$  \hspace{1cm} (3)

The measured cross section is obtained by convoluting Eq. (1) with the flux $f_{\gamma,e}(z = E_\gamma/E_{\text{beam}})$ of the incoming (quasi-)real photons.

If the photon momentum $p$ is known, then not only $Q^2$ and $y$, but also $W_{\text{had}}$ and $x$ in Eqs. (2) and (3) are fixed by energy and angle of the ‘tagged’ outgoing electron, as in usual electron-proton DIS. If $p$ is unknown, the determination of $x$ has to proceed via calorimetric measurements of the hadronic final state. Beam-pipe losses then render it very difficult, if not impossible, to obtain high-precision data on $F_2^\gamma(x, Q^2)$.

## 2 Photon spectra

A ubiquitous source of quasi-real photons at an electron collider is the soft bremsstrahlung (‘Weizsäcker-Williams’) spectrum emitted by almost undeflected electrons [5]. This spectrum has been the photon source for the $F_2^\gamma$ measurements at LEP and previous $e^+e^-$ colliders [6], where the corresponding electrons are undetected (‘anti-tagged’). In order to determine the momenta of the quasi-real photons, however, as required for precision measurements of $F_2^\gamma$, these forward electrons need to be tagged as well. Due to the high beam energies $E_b$ at a linear collider this should be done at angles $\theta_f \lesssim 2 \text{ mrad}$, restricting the high-virtuality tail of the WW spectrum which reaches up to $P^2 \equiv -p^2 \simeq (1 - z) E_b^2 \theta_f^2$. It seems not too likely that this can be achieved with high accuracy and efficiency.

For an optimistic estimate of possible event numbers in this scenario we will assume a 10% efficiency for $0.2 E_b \leq x \leq 0.8 E_b$. Thus we use

$$f_{\gamma,e}^{\text{WW}}(z) = K \theta(z - 0.2) \theta(0.8 - z)$$

$$\frac{\alpha}{\pi z} \left[ (1 + (1 - z)^2) \ln \frac{E_b \theta_f (1 - z)}{m_e z} - (1 - z) \right]$$

\hspace{1cm} (4)

with $K = 0.1$ and $\theta_f = 2 \text{ mrad}$. 

3
A very appealing new possibility envisaged for the linear collider is to operate the machine as an $e\gamma$ collider as well. This can be realized by converting one of the electron beams to a real-photon beam by backscattering of laser photons [7]. Subsequently the resulting broad spectrum can be transformed into a rather monochromatic photon beam,

$$E_\gamma \approx 0.8 E_b \ \Delta E_\gamma \approx 0.1 E_\gamma,$$

under suitable machine conditions, see ref. [8].

For our illustrations below we will employ a simple model spectrum [2] incorporating Eq. (5) and the rough shape of the high-$z$ peak:

$$f_{\gamma/e}^{\text{BL}}(z) = K' \theta(z-0.63) \theta(0.83-z) 375 (z-0.63)^2$$ (6)

with $K' = 0.1$. The latter suppression factor leads to a conservative estimate of the attainable $e\gamma$ luminosity. The flux functions (4) and (6) are compared in Fig. 2.

![Figure 2: The effective flux functions for bremsstrahlung (WW) and backscattered laser (BL) photons given in Eq. (4) and Eq. (6), respectively.](image-url)
Figure 3: Expected event numbers of $e\gamma$ DIS for bremsstrahlung photons at a 500 GeV linear collider. Forward-electron tagging is assumed to be possible with 10% efficiency for $\theta_f \leq 2$ mrad and electron energies between 50 and 200 GeV.

3 Event numbers

The kinematic coverage for measurements of $F_2^\gamma(x,Q^2)$ strongly depends on the minimal angle $\theta_{\text{tag, min}}$ down to which the scattered electron can be detected. In fact, an electron tagger inside the radiation shielding masks of the main detector at about 10 degrees is indispensable for accessing the region $Q^2 < 1000$ GeV$^2$ at a 500 GeV machine. Presently $\theta_{\text{tag, min}} = 25$ mrad is considered feasible, a value even below the 40 mrad demanded in ref. [2]. Also important is the background suppression cut $E_{\text{tag, min}}$ on the energy of the scattered electron. For the present study we replace the previous choice $0.5E_b$ by the weaker requirement $E_{\text{tag, min}} = 50$ GeV. The accessible $y$-range is thus enlarged from $y \leq 0.5$ to $y \leq 0.8$.

The resulting event numbers are shown in Fig. 2 for the bremsstrahlung scenario (4), and in Fig. 4 for the laser backscattering scenario (6). $F_2^\gamma_L$ in Eq. (1) are calculated using the leading-order GRV parametrisation [9]. An integrated $e^+e^-$ luminosity of 200 fb$^{-1}$, typical for the present TESLA design,
Figure 4: Expected event numbers of electron-photon DIS for the backscattered-laser $e\gamma$ mode of a 500 GeV linear collider. It is assumed that 10% of the $e^+e^-$ luminosity can be reached in this mode for a rather monochromatic photon beam. 

is assumed. In both cases this luminosity is effectively reduced by a factor of 10 by the $f_{\gamma,e}$ assumptions in Sect. 2. Under these conditions the $e\gamma$ collider is, as expected from Fig. 2, vastly superior to the WW scenario. E.g., the difference in the high-$Q^2$ reach at large $x$ amounts to one order of magnitude.

4 $F_2^\gamma$ measurements

The maximal accuracies for $F_2^\gamma$ determinations are illustrated in Fig. 5 for the preferred $e\gamma$ case (also reported in [10]). Here we have assumed that the systematic error is equal to the statistical one inferred from the event numbers, but amounts to at least 3%. For the present parameters, precision measurements are possible at large $x$ for $40 \text{ GeV}^2 \lesssim Q^2 \lesssim 10^4 \text{ GeV}^2$. The region $Q^2 < 30 \text{ GeV}^2$ can only be reached by a (preferably asymmetric) lower energy run. However, such $Q^2$-values can be accessed at very small $x$. Only in this region, $x \approx 10^{-4}$, the cross section (1) receives noticeable
Figure 5: The possible kinematic coverage and maximal accuracy of the measurement of $F_2^{\gamma}$ for the backscattered-laser $e\gamma$ mode at a 500 GeV linear collider. The open circles show the bins with an expected $F_L^{\gamma}$-effect of 10% or more. The sources of the extended $x$ and $Q^2$ reach with respect to the 1995 study [2] are indicated. The values of $F_2^{\gamma}$ have been scaled by the factors given in the figure.

Contributions from the longitudinal structure function $F_L^{\gamma}$.

Charm production contributes about 30–40% to the cross section over almost the entire kinematic region of Fig 4. A decent measurement of $F_2^{\gamma}$ should thus be possible at large $x$, where the final-state particles are not too forward.

Fig. 6 show the $F_2^{\gamma}$ after an additional cut of $y \geq 10^{-3}$ and for systematic errors of 5%. The cut in $y$ results from the inability to measure $y$ below that value due to the energy resolution of the electron tagger and the forward kinematics of the current jet. It is determined extrapolating techniques used at HERA and proposed for a TESLA-HERA $e\gamma$ collider [11]. The systematic errors are determined with SIMDET [12] studies and by extrapolating
Figure 6: The possible kinematic coverage and maximal accuracy of the measurement of $F_2^\gamma$ for the backscattered-laser $e\gamma$ mode at a 500 GeV linear collider. An additional cut in $y$ is imposed and the systematic errors amount to 5%. The values of $F_2^\gamma$ have been scaled by the factors given in the figure.

The dependence of the large-$x$ evolution of $F_2^\gamma$ on the strong coupling constant $\alpha_s$ is quite different from that of hadronic structure functions. The latter case is recalled in Fig. 7 where the NLO pion parametrisation of ref. [13], after transformation to the DIS scheme at $Q^2 = 4 \text{ GeV}^2$, is evolved for four
flavours. The $\alpha_s$-sensitive quantities are the logarithmic $Q^2$-slopes of $F_2$ at large $x$; an overall normalization error is irrelevant.

The corresponding results for the photon case are illustrated in Fig. 8 using the parametrisation of ref. [9]. Here the $\alpha_s$-sensitive quantities are the absolute values of $F_2^\gamma$ at very large-$x$ and high $Q^2$, cf. ref. [14]. At $x = 0.8$, e.g., a change of $\alpha_s(M_Z)$ by 5% leads to an effect of about 3% on $F_2^\gamma$.

![Figure 7](image.png)

**Figure 7**: The $\alpha_s$-dependence of the large-$x$ NLO evolution of the neutral-pion structure function $F_2^\pi$ for a fixed input at $Q^2 = 4\text{ GeV}^2$. The dotted lines show the effect of input normalization offsets of $-3\%$ and $-10\%$ on the $\alpha_s(M_Z) = 0.115$ curves.
Figure 8: As Fig. 7, but for $F_2^\gamma$. Note the shrinking high-$Q^2$ impact of low-scale normalization changes at large $x$, and the almost identical shapes of the upper dotted ($\alpha_s(M_Z) = 0.115$) and the dash-dotted ($\alpha_s = 0.110$) curves at $x = 0.8$.

6 Conclusion

A high-energy $e\gamma$ collider, realised via Compton backscattering of laser photons at a future $e^+e^-$ collider, would be a unique source of information on the photon structure. At a 500 GeV machine the structure function $F_2^\gamma$ can be accurately measured at large $x$ for $40 \, \text{GeV}^2 \lesssim Q^2 \lesssim 10^4 \, \text{GeV}^2$. Small values of $x$ down to below $10^{-4}$ can be reached for $Q^2 \approx 10 \, \text{GeV}^2$, thus complementing the $F_2^p$ results of HERA in this regime.

At large values of $x$ and $Q^2$, $x > 0.7$ and $Q^2 > 10^3 \, \text{GeV}^3$, the absolute values of $F_2^\gamma$ become robust predictions of perturbative QCD. A competitive extraction of $\alpha_s$ from these values would require very high accuracies on both the experimental and the theoretical sides.
References


